

# GeoTox and RGCA

Developing Extensible Software for Geospatial Exposure and Risk Assessment of Chemical Mixtures

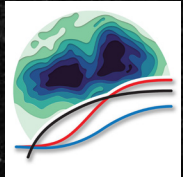
Kyle P Messier, PhD

**Stadtman Tenure Track Investigator**

National Institute of Environmental Health Sciences

Division of Translational Toxicology

February 14, 2024



# About Us: {SET}group

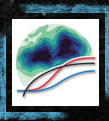
- Spatiotemporal Exposure Mapping

$$y \sim GP(X\beta, \Sigma)$$

- Chemical and Stressor Mixtures Prediction

$$\frac{[A]}{f_A^{-1}(R)} + \frac{[B]}{f_B^{-1}(R)} = 1$$

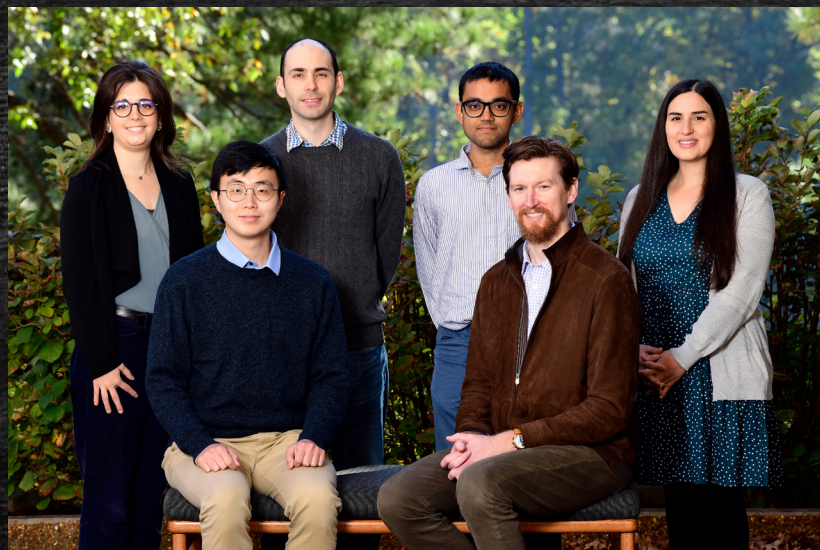
Mechanistically Informed Risk Assessment



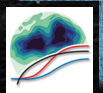
$$R = f(c|\alpha, \theta, \beta) = \frac{\alpha}{1 + \left(\frac{\theta}{x}\right)^\beta}$$



# About Us: {SET}group

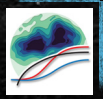
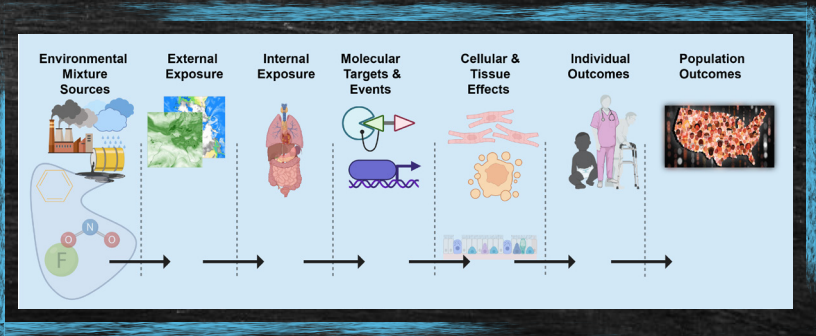


- ★ Eva Marques
- ★ Daniel Zilber
- ★ Ranadeep Daw
- ★ Mariana Alifa
- ★ Insang Song
- ★ Kyle Messier
- ★ Mitchell Manware (Not Pictured)



# A Necessary Cascade for Exogoneous Risk Factors

- Exogenous Sources
- External Exposure
- Internal Exposure
- Molecular Targets and Events
- Cellular and Tissue Effects
- Individual Outcomes
- Population Outcomes





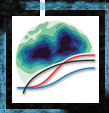
# Getting Two Frameworks to Work Together

## Aggregate Exposure Pathways

AEP is a comprehensive external analysis of source, media, and transformations

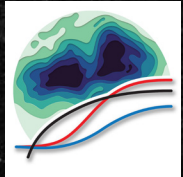
## Adverse Outcome Pathway

AOPs provide a linkage specific biological target, pathway or process by a stressor and an adverse outcome(s) considered relevant to risk assessment



# Getting Two Frameworks to Work Together

$$GeoTox = AEP + AOP$$

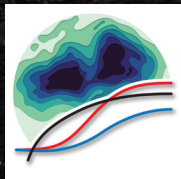




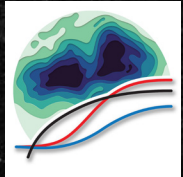
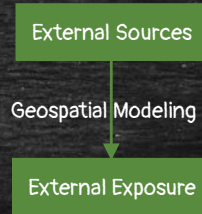
# Key Steps of GeoTox

External Sources

- A forward, exposure-based approach for mixtures risk modeling
- Exposure modeling provides a *geospatial* foundation for risk assessment

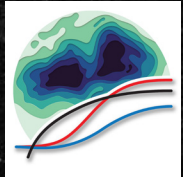
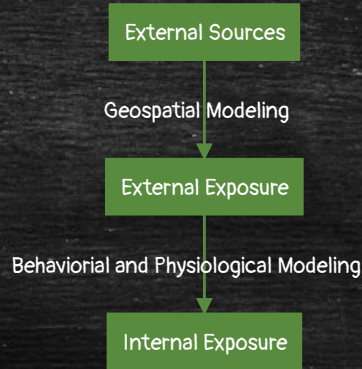


# Key Steps of GeoTox

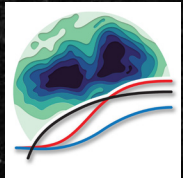
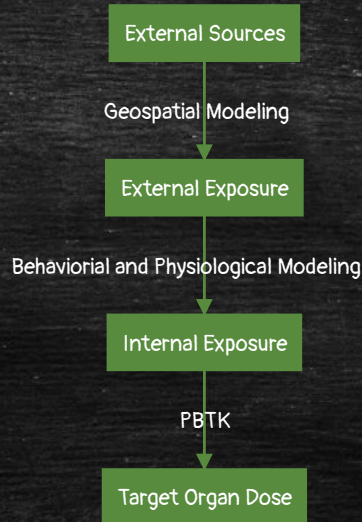




# Key Steps of GeoTox

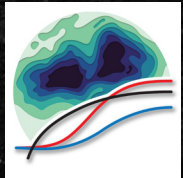
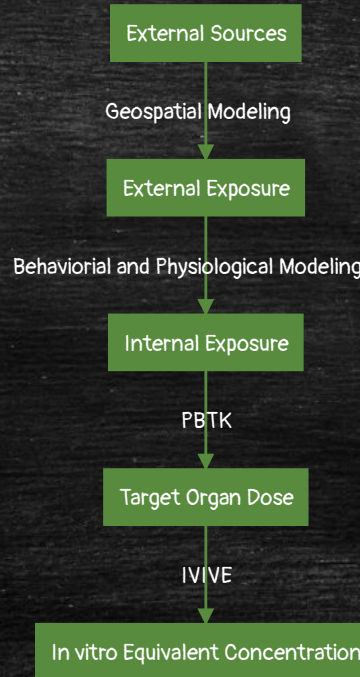


# Key Steps of GeoTox

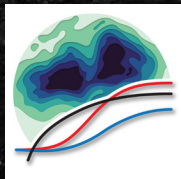
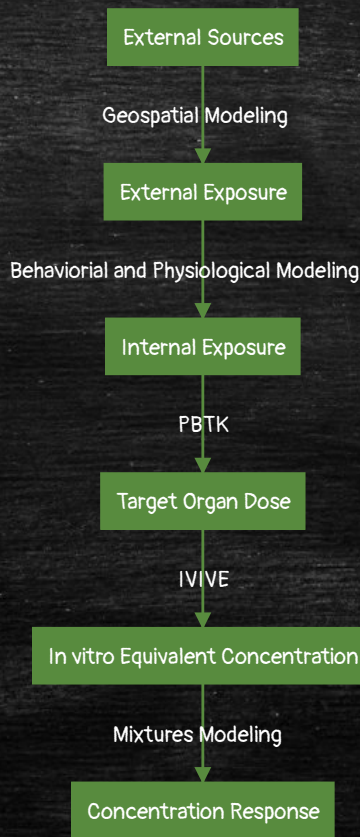




# Key Steps of GeoTox



# Key Steps of GeoTox





# GeoTox Proof of Concept

Contents lists available at ScienceDirect

Science of the Total Environment

journal homepage: [www.elsevier.com/locate/scitotenv](http://www.elsevier.com/locate/scitotenv)

**A geospatial modeling approach to quantifying the risk of exposure to environmental chemical mixtures via a common molecular target**

Kristin M. Eccles<sup>a</sup>, Agnes L. Karmaus<sup>b</sup>, Nicole C. Kleinstreuer<sup>a</sup>, Fred Parham<sup>a</sup>, Cynthia V. Rider<sup>a</sup>, John F. Wambaugh<sup>c</sup>, Kyle P. Messier<sup>a,\*</sup>

<sup>a</sup> National Institute of Environmental Health Science, Division of the Translational Toxicology, Durham, USA  
<sup>b</sup> Integrated Laboratory Systems, an Innotiv Company, Morrisville, NC, USA  
<sup>c</sup> United States Environmental Protection Agency, Center for Computational Toxicology and Exposure, Durham, USA

**HIGHLIGHTS**

- We assess the geographic variation for the joint effect of many chemical exposures.
- This example workflow integrates NAMs with chemical exposure data.
- The biological perturbations were heterogeneously distributed across space.
- Exposure concentrations, demographics, and toxicokinetics influence variability.
- We provide methods for modeling the source-exposure-effect continuum.

**GRAPHICAL ABSTRACT**

The graphical abstract illustrates a workflow for assessing the geographic variation of chemical exposures. It starts with 'Environmental Contaminants' (PAHs, PCBs, etc.) and 'High Throughput Assays' (NAMs, etc.). These are integrated into a 'Data Integration' step. This leads to 'Molecular Modeling' (Molecular Mechanisms, etc.) and 'Geospatial Modeling' (Geospatial Modeling, etc.). The final output is 'Predicted Geospatial Risk of Molecular Perturbations', which is linked to 'Molecular Mechanisms' and 'Molecular Mechanisms Pathways (MMP)'.



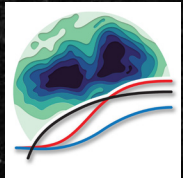
Dr. Kristin Eccles,  
Former Visiting Fellow  
in DTT and SET, Now  
at Health Canada

2022 NIEHS  
Paper of the  
Year



# Making GeoTox F.A.I.R.

- Findable: Publicly available via GitHub, CRAN, NIEHS websites
- Accessible: Open-Source, Easy installation
- Interoperable: Integrate with current and future applications
- Reusable: Documentation and reproducible pipelines





# GeoTox Development

- ✦ Currently developing (experimental or not-stable)
- ✦ Submitting to CRAN
- ✦ Static website hosted via {SET}group website
- ✦ Maintained
- ✦ Extensible for future development



Dr David Reif, Predictive Toxicology Branch, Senior Scientist and Branch Chief

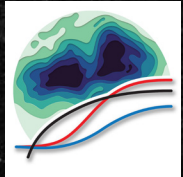


Dr Skylar Marvel, Predictive Toxicology Branch, Bioinformatic Scientist



# GeoTox: Simulating Data

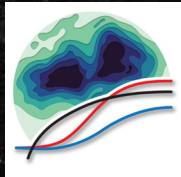
```
1 # Age
2 age <- simulate_age(split(geo_tox_data$age, ~FIPS), n = MC_iter)
3
4 # Obesity status
5 obesity <- simulate_obesity(geo_tox_data$obesity, n = MC_iter)
6
7 # Inhalation rate
8 IR <- simulate_inhalation_rate(age)
```





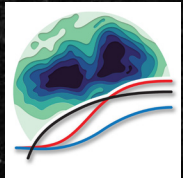
# GeoTox: Simulating Data

```
1 # Age
2 age <- simulate_age(split(geo_tox_data$age, ~FIPS), n = MC_iter)
3
4 # Obesity status
5 obesity <- simulate_obesity(geo_tox_data$obesity, n = MC_iter)
6
7 # Inhalation rate
8 IR <- simulate_inhalation_rate(age)
9
10 # External exposure concentration
11 C_ext <- simulate_exposure(split(geo_tox_data$exposure, ~FIPS), n = MC_iter)
12
13 # Sample from pre-simulated steady-state plasma concentration data
14 C_ss <- sample_Css(geo_tox_data$simulated_css, age, obesity)
```



# GeoTox: Core Functions

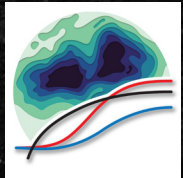
```
1 # Internal dose  
2 D_int <- calc_internal_dose(C_ext, IR, scaling = 1 / 1000)
```





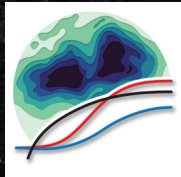
# GeoTox: Core Functions

```
1 # Internal dose
2 D_int <- calc_internal_dose(C_ext, IR, scaling = 1 / 1000)
3
4 # in vitro concentration
5 C_invitro <- calc_invitro_concentration(D_int, C_ss)
```



# GeoTox: Core Functions

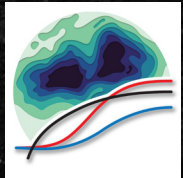
```
1 # Internal dose
2 D_int <- calc_internal_dose(C_ext, IR, scaling = 1 / 1000)
3
4 # in vitro concentration
5 C_invitro <- calc_invitro_concentration(D_int, C_ss)
6
7 # Concentration response
8 resp <- calc_concentration_response(C_invitro, hill_2_params)
```





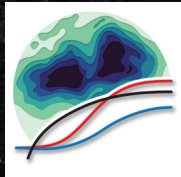
# GeoTox: Documentation

```
1 # Internal dose  
2 D_int <- calc_internal_dose(C_ext, IR, scaling = 1 / 1000)
```



# GeoTox: Documentation

```
1 # Internal dose
2 D_int <- calc_internal_dose(C_ext, IR, scaling = 1 / 1000)
```



GeoTox 0.0.0.9000

Reference

Articles ▾

Search for

## Calculate internal chemical dose

Estimate the internal dose from inhalation of a chemical given inhalation rate, time, and body weight

### Usage

```
calc_internal_dose(C_ext, IR, time = 1, BW = 1, scaling = 1)
```

### Arguments

**C\_ext**  
ambient chemical concentration in  $\frac{mg}{m^3}$

**IR**  
inhalation rate in  $\frac{m^3}{day}$

**time**  
total time in *days*

**BW**  
body weight in *kg*

**scaling**  
scaling factor encompassing any required unit adjustments

**Value**  
internal chemical dose in  $\frac{mg}{kg}$

### Details

TODO Additional details...

$$D_{int} = \frac{C_{ext} \times IR \times time}{BW}$$

### Examples

```
n_chem <- 3
n_sample <- 5

# Single population
C_ext <- matrix(runif(n_sample * n_chem), ncol = n_chem)
IR <- runif(n_sample)
calc_internal_dose(C_ext, IR)
#>      [,1]      [,2]      [,3]
#> [1,] 0.015809366 0.09125914 0.171132967
#> [2,] 0.336685183 0.20087215 0.076595211
#> [3,] 0.038245313 0.01844701 0.002179853
#> [4,] 0.061187128 0.28487219 0.124534354
#> [5,] 0.007218509 0.75363169 0.392498442
```

On this page

Usage

Arguments

Value

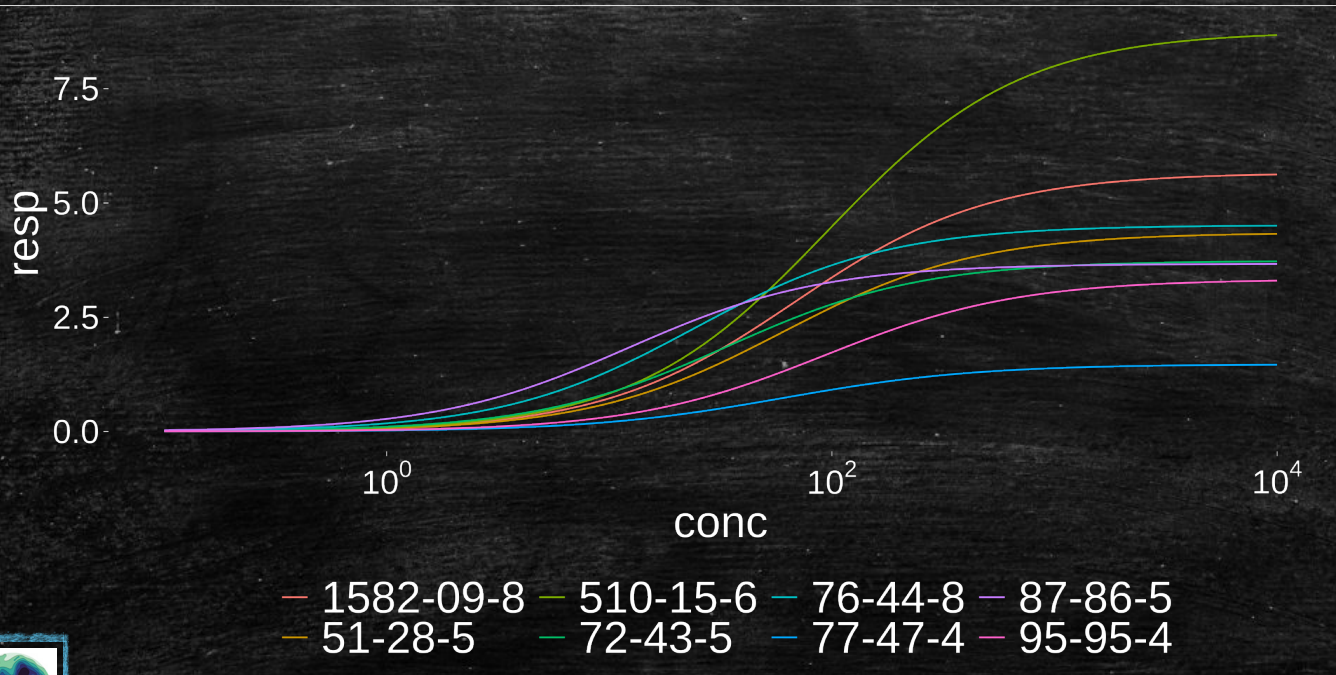
Details

Examples



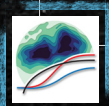
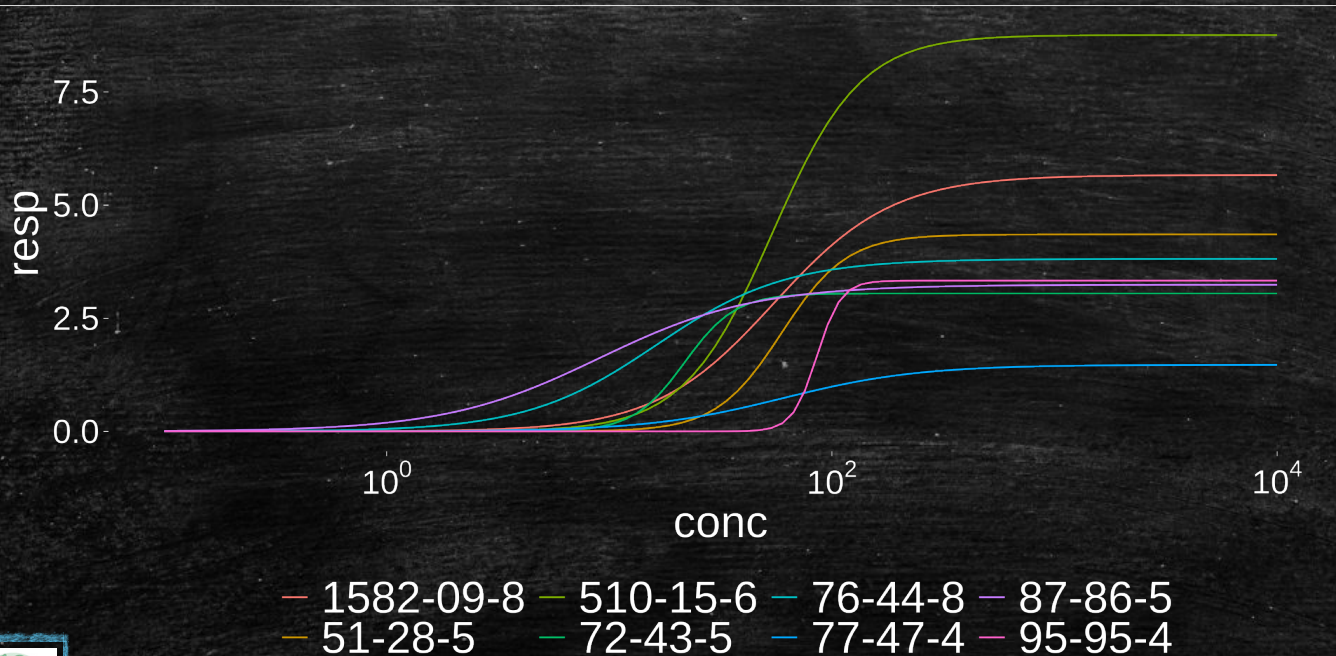
# GeoTox: Dose-Response

```
1 hill_2_params <- fit_hill(data)
2 plot_hill(hill_2_params)
```



# GeoTox: Dose-Response

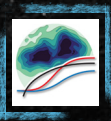
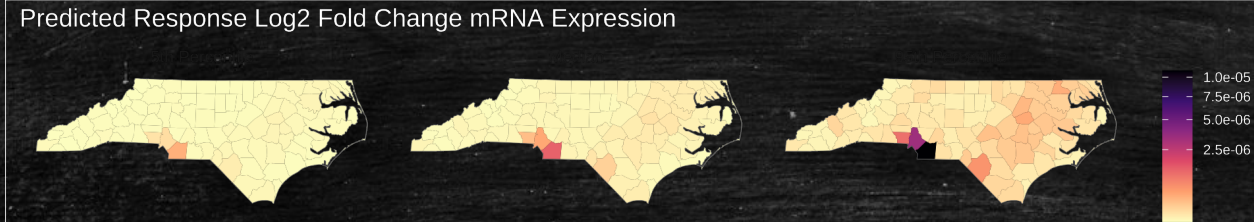
```
1 hill_3_params <- fit_hill(data, fixed_slope = FALSE)
2 plot_hill(hill_3_params)
```





# GeoTox: Map Visualization

```
1 resp <- resp_df %>% filter(health_measure == "GCA.Eff")  
2 legend_name <- paste("Predicted Response", "Log2 Fold Change", "mRNA Expression", sep = " ")  
3 make_county_heatmap(resp, legend_name)
```



# GeoTox: Under Development

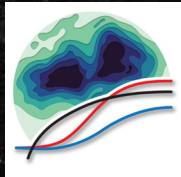
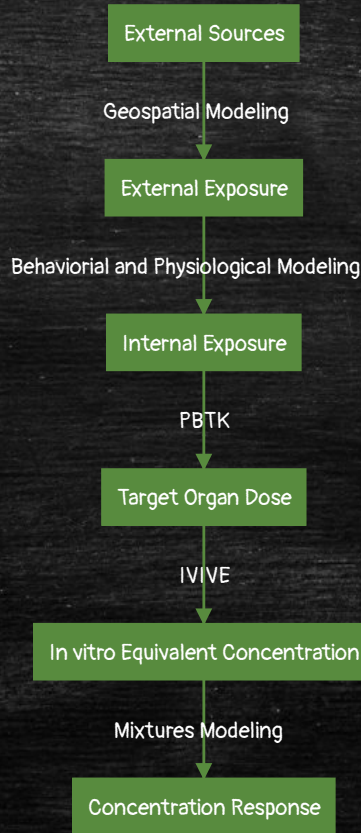
lifecycle experimental

- Individual/Person Level Analysis
- General Grouping or Areal Analysis
- Likely migrating to an object-oriented approach

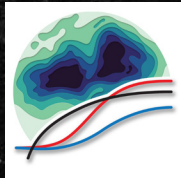
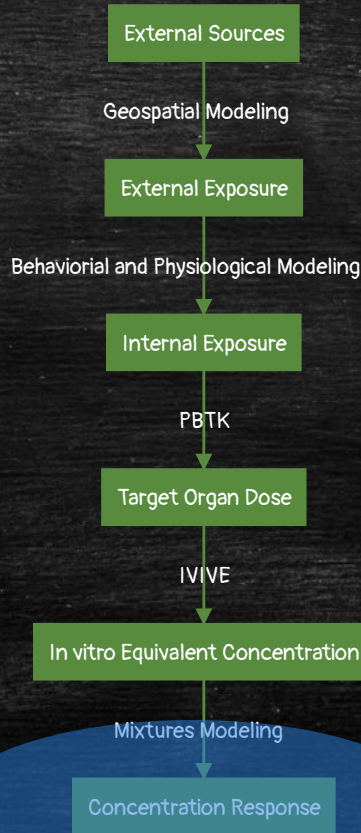




# Revisiting the Steps of GeoTox

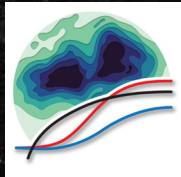


# Revisiting the Steps of GeoTox



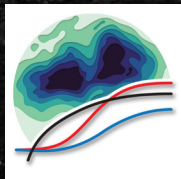


# Revisiting the Steps of GeoTox



# RGCA Motivation

- ❖ *Infinite Mixture Problem*: There are infinitely many possible mixtures and we can't test them all
- ❖ *Independent vs Additive*: No clear approach for general mixtures
- ❖ *Something from Nothing*: Independently safe chemicals can combine to form a hazardous mixture





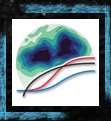
# RGCA: Notation

We assume a parametric model for interpretability:

$$r_i(c) = f_i(c|a_i, \theta_i, \beta_i) = \frac{a_i}{1 + \left(\frac{\theta_i}{c}\right)^{\beta_i}}$$

where:

- ✿  $r_i$ : toxic effect or response of chemical  $i$
- ✿  $c$ : concentration of a chemical, later indexed by chemical  $i$
- ✿  $a_i$ : sill or maximum effect parameter
- ✿  $\theta_i$ : dissociation constant or EC50 value
- ✿  $\beta_i$ : slope parameter



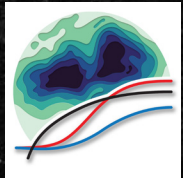
# RGCA: Common Mixture Models

- ◆ Concentration Addition, CA (Loewe, Isobole): effective total dose adjusted for potency

$$\sum_i \frac{c_i}{EC_i(R)} = 1$$

Intuition: “How much  $c_2$  do I need to get response  $R$  under chem 1 given  $c_1$ ”

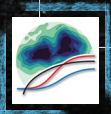
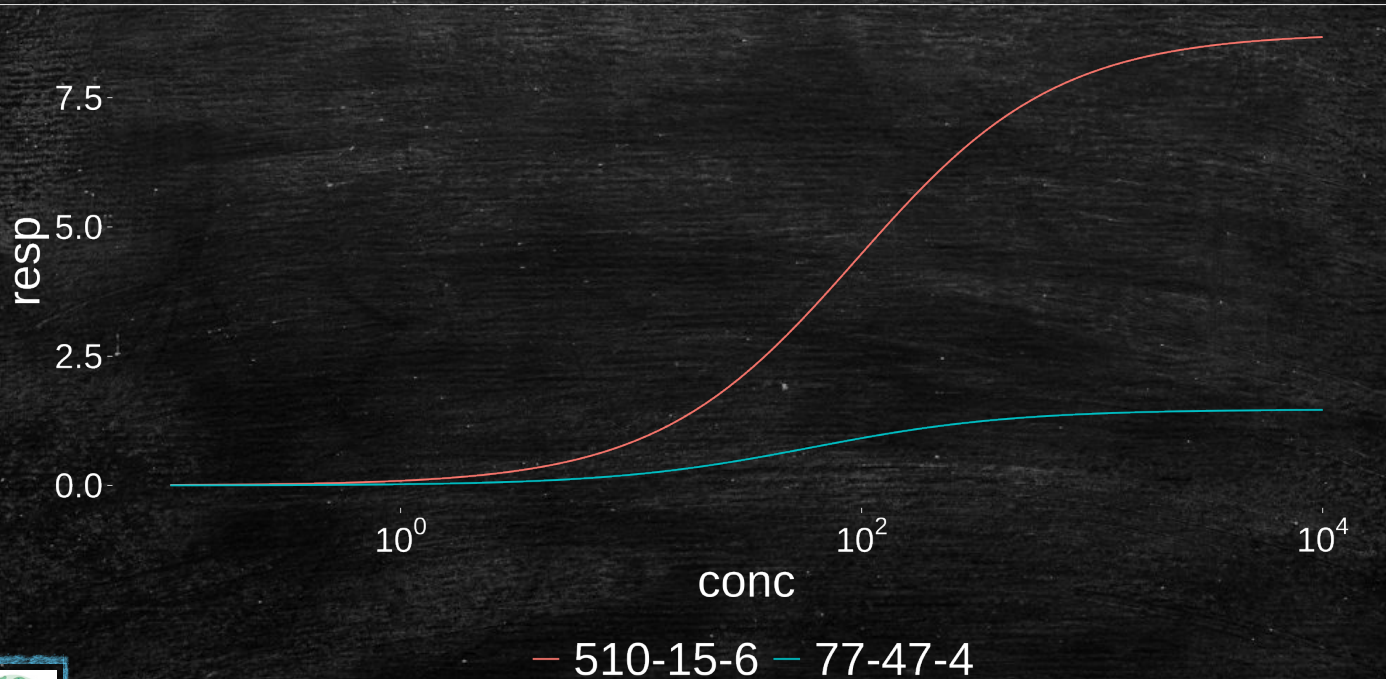
$$EC_1(R) = c_1 + c_2 \frac{EC_1(R)}{EC_2(R)}$$





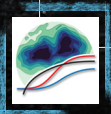
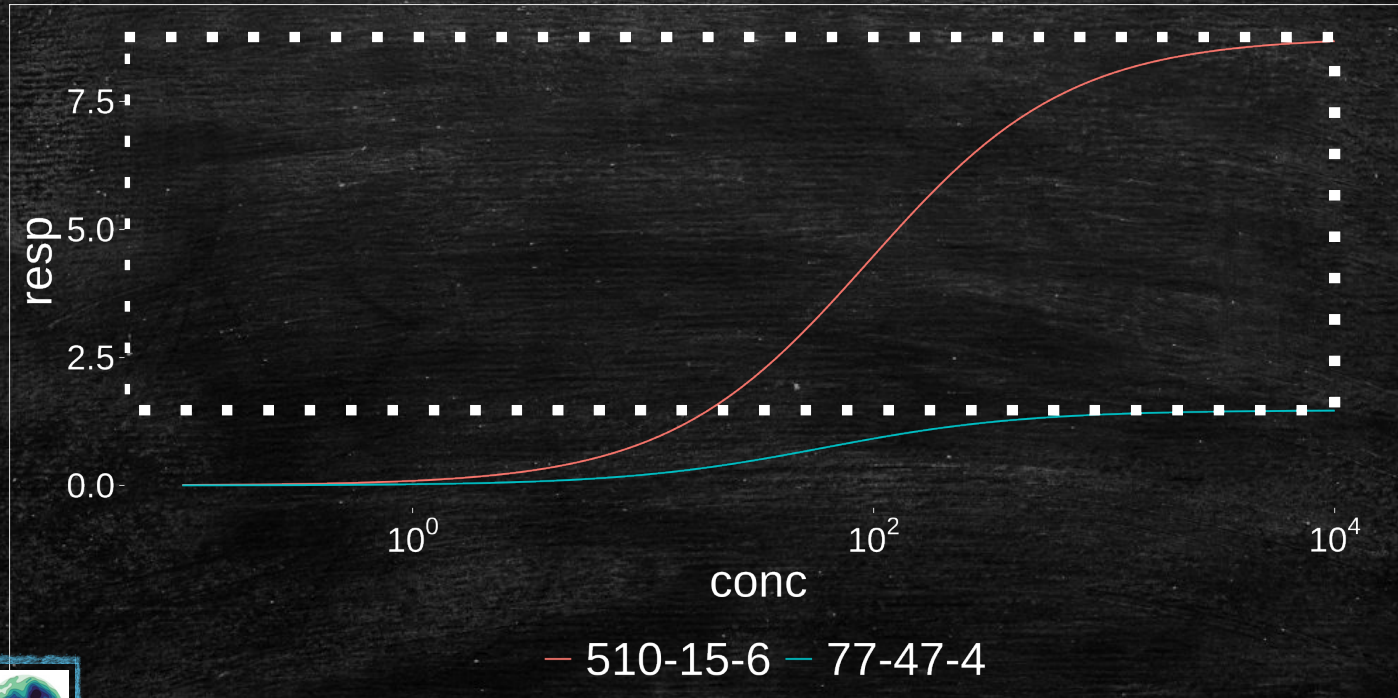
# RGCA: Partial Agonists

Partial agonists are the major limitation of traditional CA



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# RGCA: Partial Agonists

GCA (Howard and Webster, 2009) substitutes  $f_i^{-1}(R)$  for  $EC_i(R)$  and solves for  $R$  to balance the equation given  $c_i$ 's:

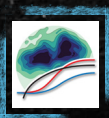
$$\sum_i \frac{c_i}{f_i^{-1}(R)} = 1$$

❖ For the Hill model with slope  $\beta_i = 1$ , we get a hyperbolic function:

$$R = f_i(c) = \frac{a_i}{1 + \left(\frac{\theta_i}{c}\right)^{\beta_i}} = \frac{c \cdot a_i}{c + \theta_i}$$

❖ So: when  $R > a_1$ ,  $c < 0$ !

❖ A large toxic effect of the mixture requires small concentrations of chemical 1.

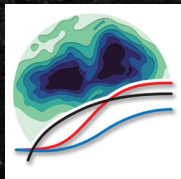


# RGCA: Partial Agonists

The GCA trick can be used with  $\beta = 1$  because the inverse is still defined for  $R > a$ :

$$f^{-1}(R) = \frac{\theta}{\left(\frac{a}{R} - 1\right)^{1/\beta}} = \frac{\theta}{\frac{a}{R} - 1}$$

For most  $\beta$ , the inverse at  $R > a$  is undefined because it contains a root of a negative value. We propose a series of reflections to have a well-defined inverse



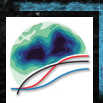


# RGCA: Piecewise Inverse Function

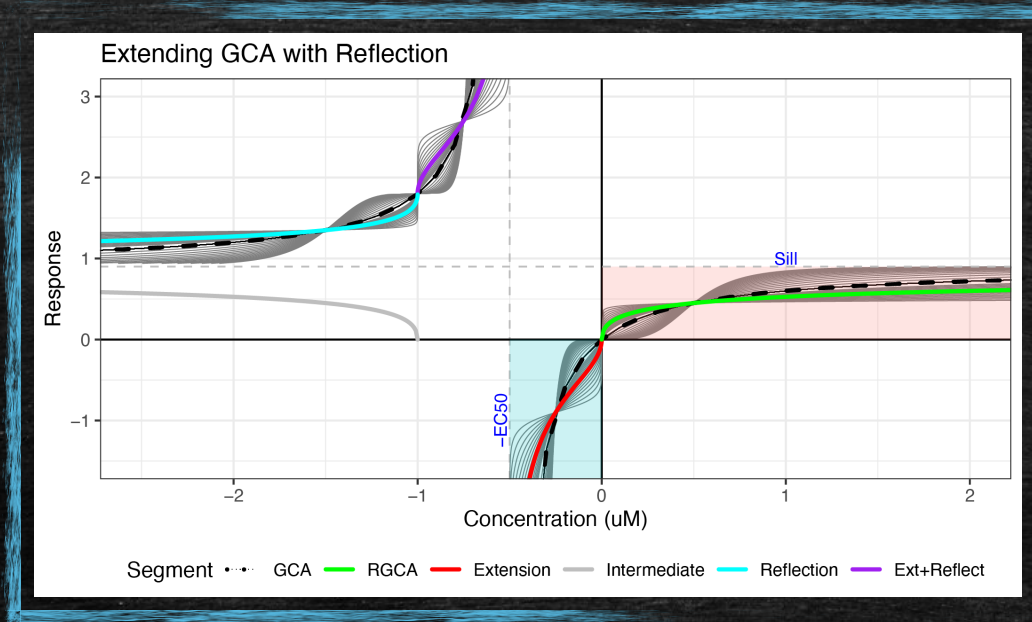


$$f^{-1}(r|\alpha > 0, \theta, \beta > 0) = \begin{cases} \frac{-\theta}{1 + \left(\frac{-\alpha}{r}\right)^{1/\beta}} & r \in (-\infty, 0) \\ \theta \left(\frac{\alpha}{r} - 1\right)^{-1/\beta} & r \in [0, \alpha) \\ -2\theta - \theta \left(\frac{\alpha}{2\alpha - r} - 1\right)^{-1/\beta} & r \in (\alpha, 2\alpha) \\ -2\theta + \frac{\theta}{1 + \left(\frac{\alpha}{r - 2\alpha}\right)^{1/\beta}} & r \in (2\alpha, \infty) \end{cases}$$

Daniel Zilber, PhD,  
Postdoctoral Fellow



# RGCA: Piecewise Inverse Function

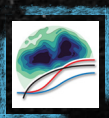


This inverse provides a wide enough support to satisfy the invertibility requirements of GCA



# RGCA: Summary

- ❖ IA and CA represent two extremes of mixture prediction
- ❖ GCA extends CA to partial agonists but requires a slope of 1
- ❖ We can extend GCA to not require slope 1: RGCA
- ❖ Non-unit slope allows for additional post-hoc analyses like clustering on slope, curve, etc.
- ❖ Daniel Zilber and Kyle P Messier, *Reflected Generalized Concentration Addition and Bayesian Hierarchical Models to Improve Chemical Mixture Prediction*, PLOS One, In-Press



# RGCA: Future Work

Both IA and CA are additive: there is no interaction. One approach is to rescale GCA (Jonker et al. 2005):

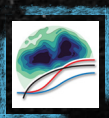
$$\sum \frac{c_i}{f_i^{-1}(R)} = \exp g(Z), \quad g(Z) = a \prod z_i$$

where the  $z_i$  is a toxic unit,  $z_i = c_i/f_i^{-1}(a/2)$ .

We considered the following quadratic version, with a matrix  $A$  to be specified by QSAR:

$$g(Z) = -\frac{1}{2}z^T A z$$

But it is not clear how to determine  $A$  from QSAR. Also, this approach is symmetric: there is no dominant chemical.





# RGCA: Extensible Software

RGCA 1.0.0.0000

[Get started](#)

[Reference](#)

## RGCA

Reflected Generalized Concentration Addition: A geometric, piecewise inverse function for 3+ parameter sigmoidal (e.g. hill) models used in chemical mixture concentration-response modeling

### Key Inverse Function:

$$f^{-1}(r|\alpha > 0, \theta, \beta > 0) = \begin{cases} \frac{-\theta}{1 + (\frac{-\theta}{r})^{1/\beta}} & r \in (-\infty, 0) \\ \theta(\frac{\alpha}{r} - 1)^{-1/\beta} & r \in [0, \alpha) \\ -2\theta - \theta(\frac{\alpha}{2\alpha - r} - 1)^{-1/\beta} & r \in (\alpha, 2\alpha) \\ -2\theta + \frac{\theta}{1 + (\frac{\alpha}{r - 2\alpha})^{1/\beta}} & r \in (2\alpha, \infty) \end{cases}$$

This inverse provides a wide enough support to satisfy the invertibility requirements of GCA, but with non-unit slopes. The resulting inverse maintains a coarse hyperbolic shape and continuity and is smooth at the transitions. This procedure is not limited to the Hill function and can be applied to any monotonic dose response function, but the resulting stability may vary. Note that negative slope parameters for the Hill function are not supported.

### Abstract:

Environmental toxicants overwhelmingly occur together as mixtures. The variety of possible chemical interactions makes it difficult to predict the danger of the mixture. In this work, the classical two-step model for the cumulative effects of mixtures, which assumes a combination of GCA and independent action (IA). We explore how various clustering methods can dramatically improve predictions. We compare our technique to the IA, CA, and GCA models and show in a simulation study that the two-step approach performs well under a variety of true models. We then apply our method to a challenging data set of individual chemical and mixture responses where the target is an androgen receptor (Tox21 AR-luc). Our results show significantly improved predictions for larger mixtures. Our work complements ongoing efforts to predict environmental exposure to various chemicals and offers a starting point for combining different exposure predictions to quantify a total risk to health.

### Links

[Browse source code](#)

### License

GPL (>= 2)

### Citation

[Citing RGCA](#)

### Developers

Daniel Zilber

Author, maintainer 

Kyle Messier

Author 

### Dev status

 R-CMD-check passing

 lint passing

 codecov 0%

 lifecycle experimental



# RGCA: Extensible Software

## Simple Application of RGCA

Daniel Zilber

Source: [vignettes/Simple\\_RGCA.Rmd](#)

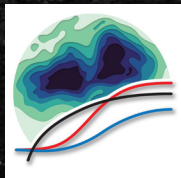
## Simple Usage of RGCA

While the method could be generalized to a variety of smooth, monotone dose response functions, our package is designed around the Hill function,

$$f(x|a,b,c) = \frac{a}{1 + \left(\frac{b}{x}\right)^c}$$

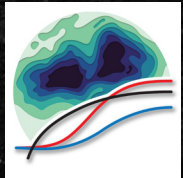
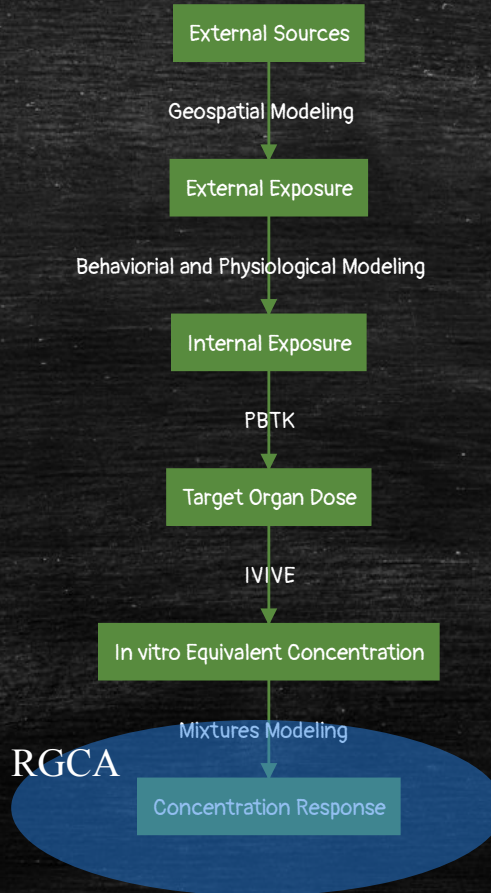
The parameters are the sill (a), the EC50 (b), and the slope (c). Give these parameters and a cluster assignment vector, RGCA can create a calculator that predicts the mixture response given an input dose vector ( $x_1, \dots, x_n$ ). In the example below, there are three chemicals with known Hill parameters.

```
n_chems <- 3
sills <- c(3, 5, 4)
ec50_vec <- c(1, 0.75, 2.4)
slopes <- c(0.5, 1.1, 2.0)
# Rmax is used to scale IA across clusters, can copy sills
param_matrix <- as.matrix(cbind("a" = sills,
                                "b" = ec50_vec,
                                "c" = slopes,
                                "max_R" = sills))
# specify both chems in cluster 1 of 1
cluster_assign_vec <- c(1, 2, 1)
# create a calculator to predict response given concentration
mix_pred <- mix_function_generator(param_matrix, cluster_assign_vec)
```





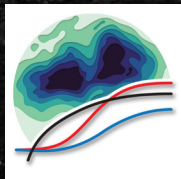
# GeoTox + RGCA Integration



# Extensible GeoTox

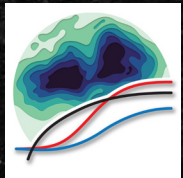
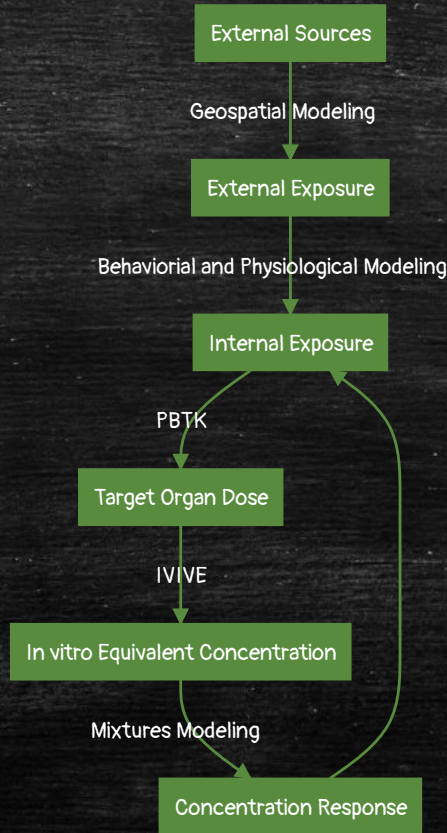
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- ◆ Looking forward, there are many ways to improve GeoTox mixture risk assessment
- ◆ Better handling of *time*
- ◆ More and better resolved AOPs!

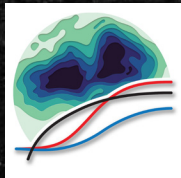




# GeoTox: Temporal Feedback

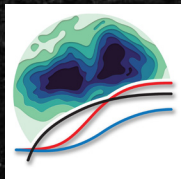
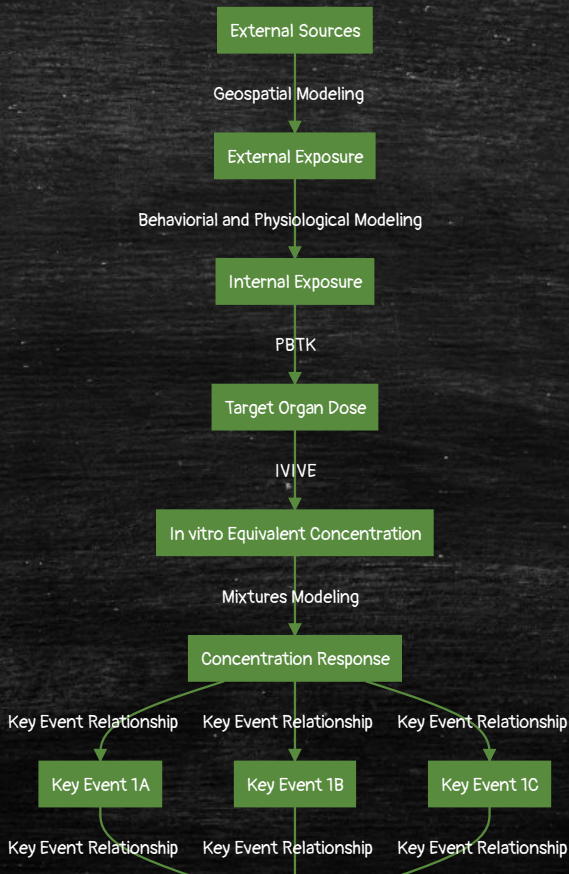


# GeoTox: With Complete AOPs



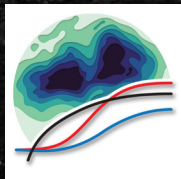


# Multiple Assays Informing an AOP



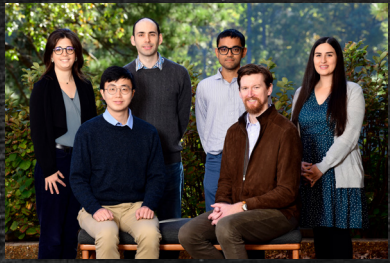
# {SET} Summary

- ❖ GeoTox and RGCA code are currently experimental
- ❖ Publishing versions 1.0.0. to SET Github and CRAN ASAP
- ❖ Many other documented, test-driven, and extensible packages from the SET group on air pollution exposures across the US, download/process GIS environmental data, and scalable GIS operations
- ❖ Follow *Spatiotemporal-Exposures-and-Toxicology* on GitHub
- ❖ We are fostering a community around best-practices for software in geospatial exposure assessment, risk assessment, and computational toxicology
- ❖ email: [kyle.messier@nih.gov](mailto:kyle.messier@nih.gov)

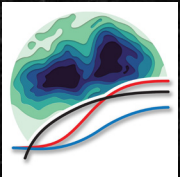




# Acknowledgements



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